

# Towards neutrino mass determination in traps

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# Masses of oscillating neutrinos

The  $\beta$ -decay/capture neutrino effective mass:

$$m_\nu(\beta) = \{a \cdot m_1^2 + b \cdot m_2^2 + c \cdot m_3^2\}^{1/2}$$

States of oscillating neutrinos:

$$|v_\alpha\rangle = \sum U_{\alpha i} |v_i\rangle \quad , \quad \text{where } i = 1, 2, 3; \quad \alpha = e, \mu, \tau \text{ - flavor}$$

A probability of flavor change :

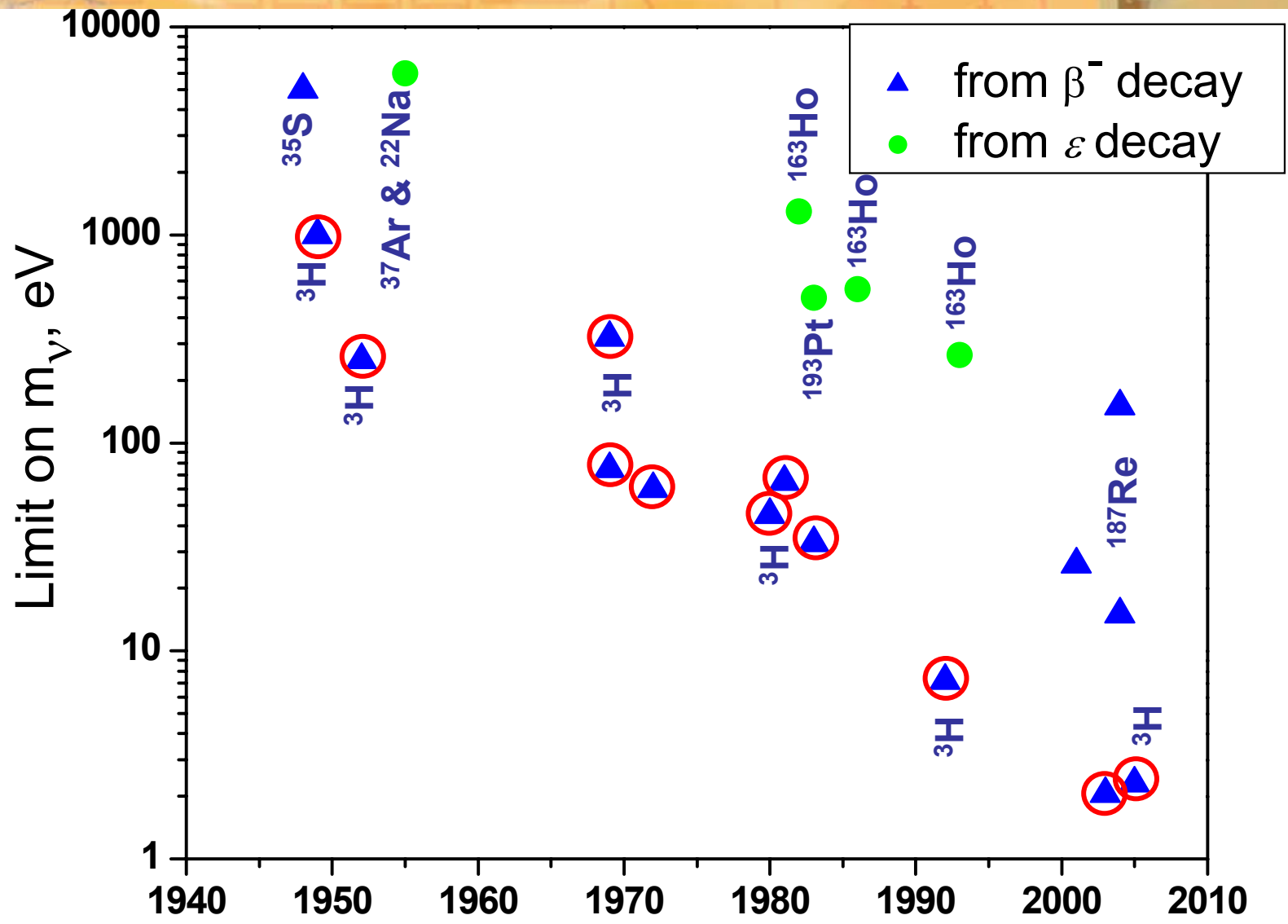
$$\Lambda = \sin^2(2\theta) \cdot \sin^2\{1.27 \Delta m^2 \cdot L/E\} \quad [\text{eV}^2 \cdot \text{m}/\text{MeV}]$$

Experimentally are determined:

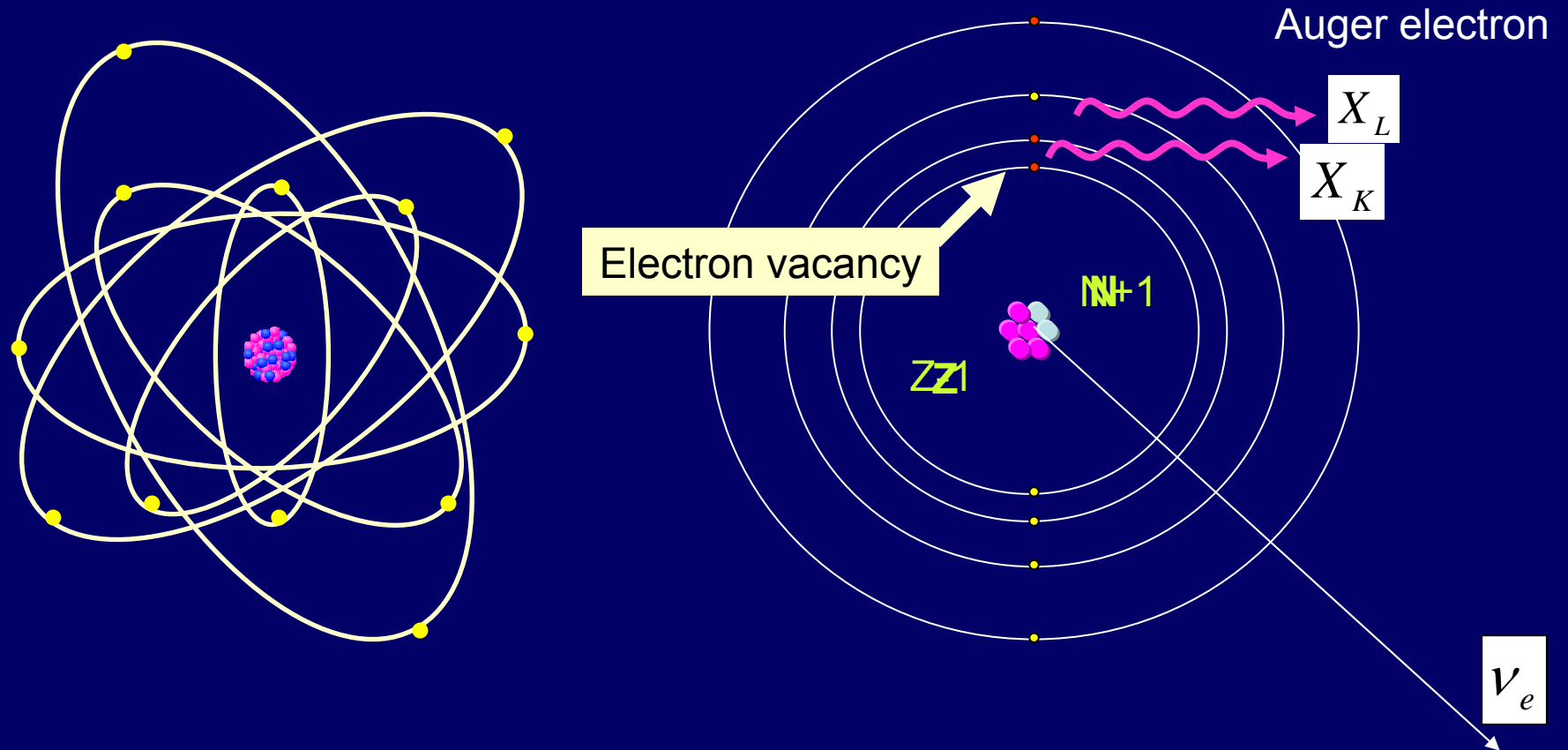
for the mixing angle -  $\tan^2\theta = 0.4$ ;

for mass difference squared  $\Delta m^2 = m_2^2 - m_1^2 = 8.2 \cdot 10^{-5} \text{ eV}^2$ .

# History of $m_\nu$ measurements



# Atomic process



start

Time range

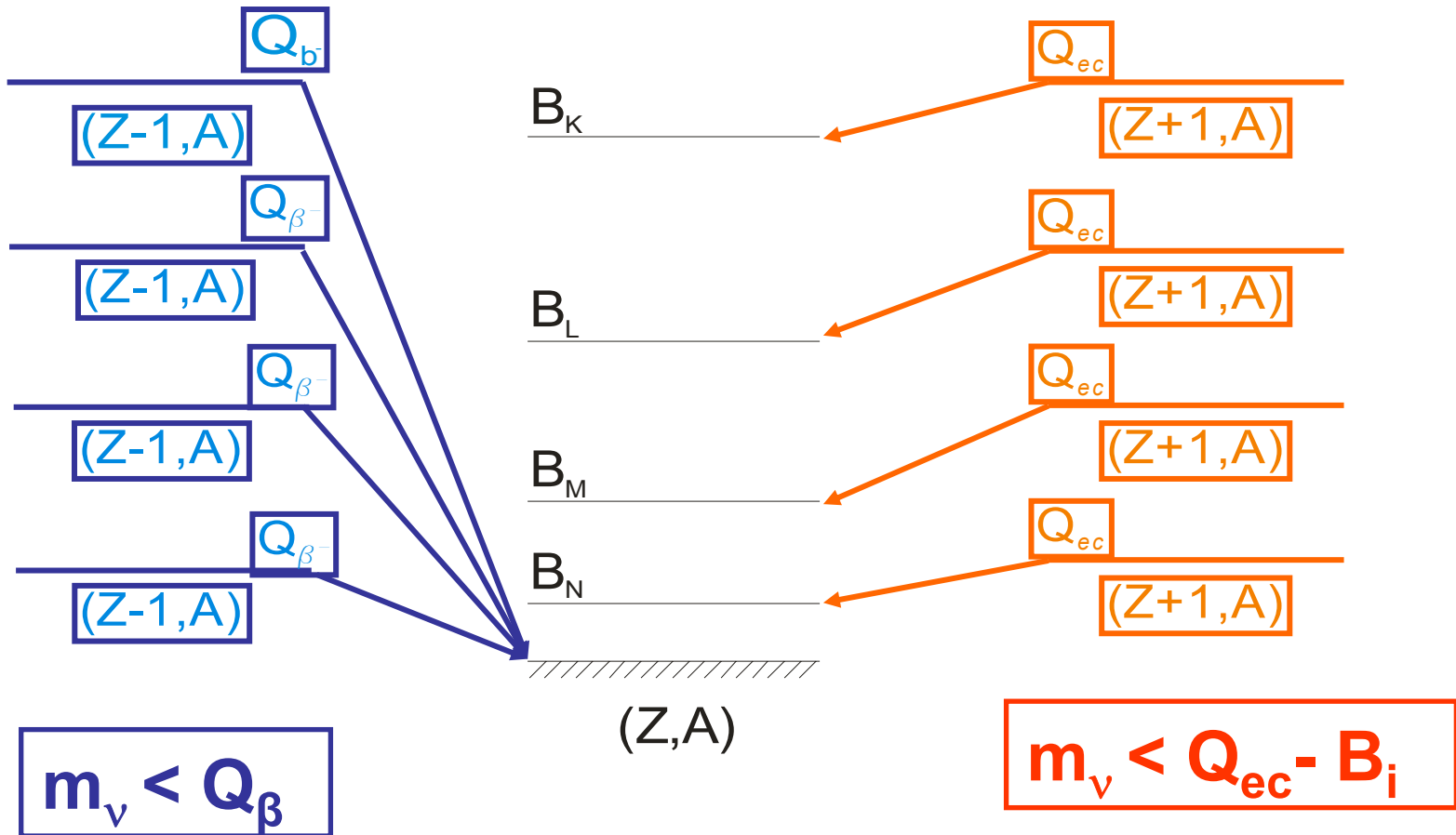
0

$10^{-18}$ s

$10^{-10}$ s

courtesy of J. Khuyagbaatar (GSI)

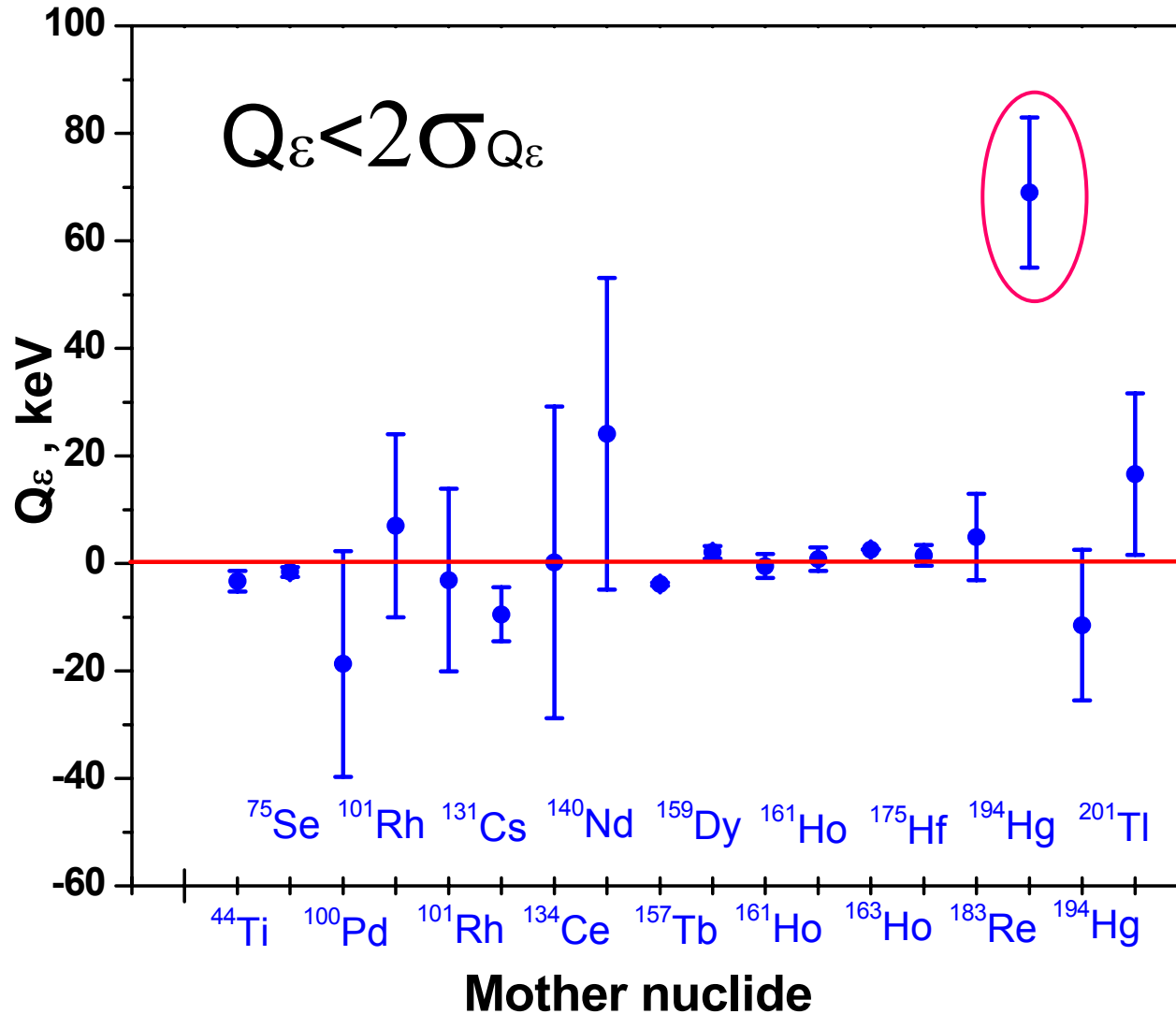
# Differences in the neutrino mass determination in $\beta^-$ and $ec$ - processes



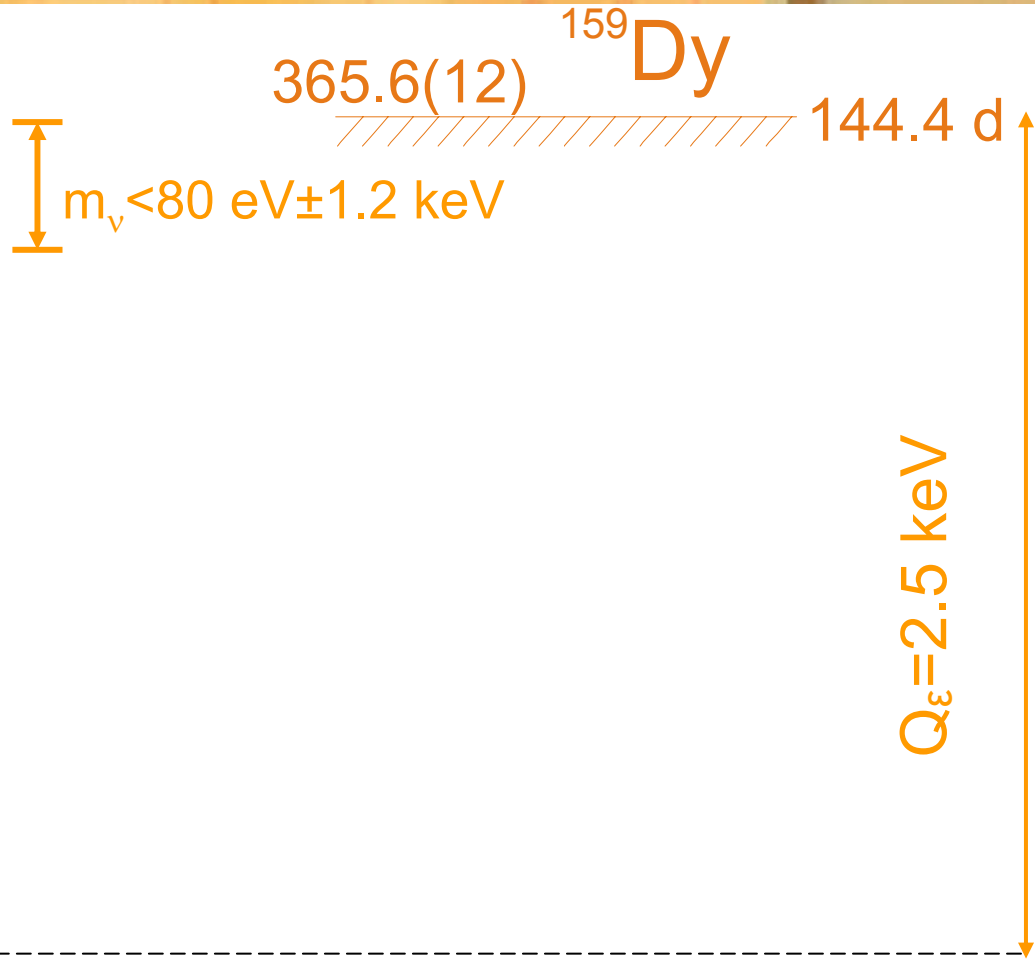


# First possibility

# Nuclides with the smallest $\varepsilon$ -energies



+1.9675	M <sub>1</sub>
+1.7677	M <sub>2</sub>
+1.6113	M <sub>3</sub>
+1.2750	M <sub>4</sub>
+1.2412	M <sub>5</sub>
+0.3979	N <sub>1</sub>



363.5449(14) keV

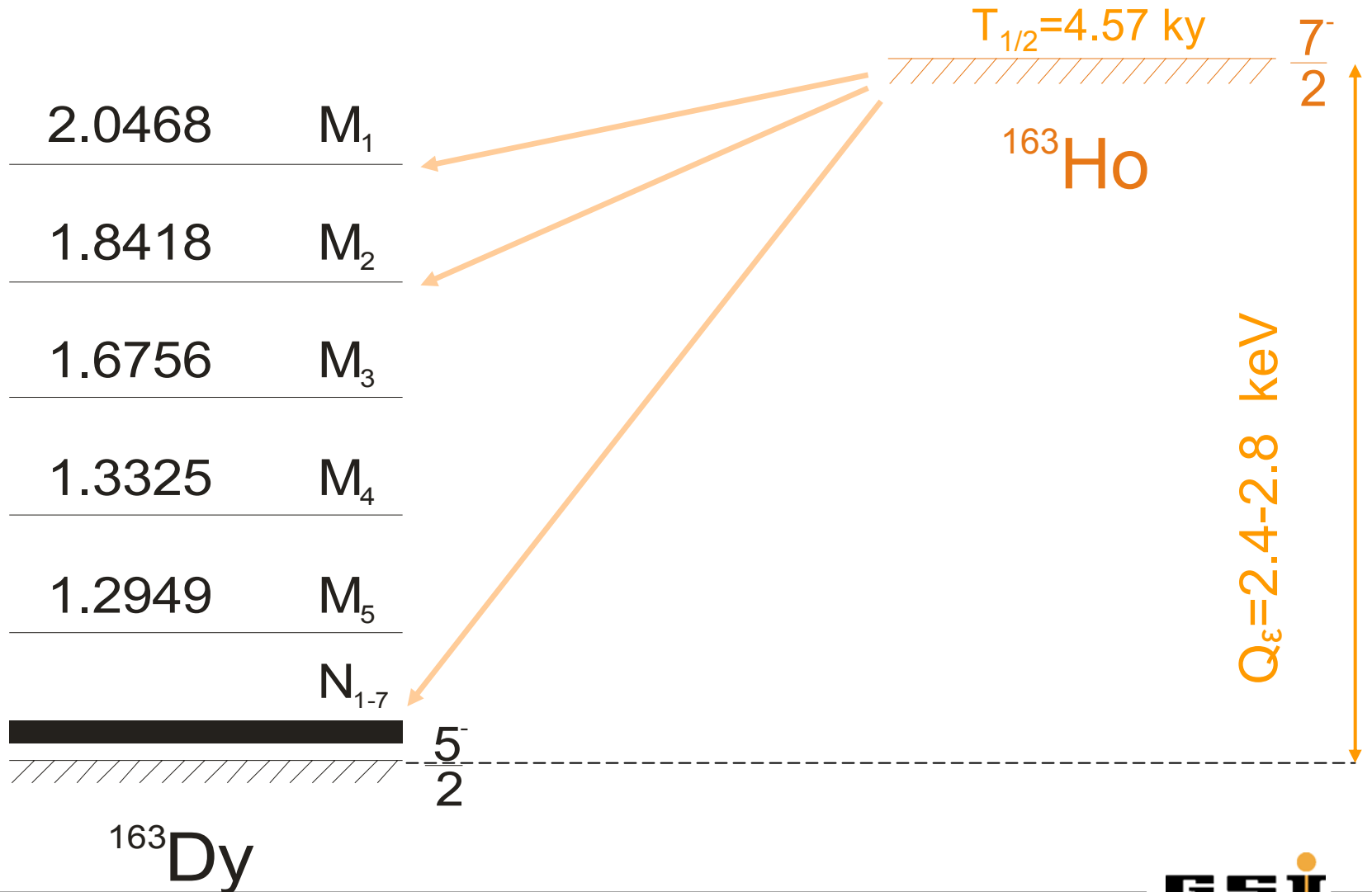
<sup>159</sup>Tb





# Second possibility

# Example for an electron-capture nuclide



# How can we derive the neutrino mass from electron-capture ?

**Total capture probability for allowed transition:**

$$\Lambda = \frac{1}{4} g^2 \pi^2 \{M_0(1,1)^2 + M_1(1,1)^2\} \sum_i n_i W_i \beta_i^2 B_i$$

**Capture ratios for “2” and “1” atomic levels:**

$$\frac{\lambda_2}{\lambda_1} = \eta \frac{W_2}{W_1} \frac{q_2}{q_1}, \text{ where}$$

$$W_i = Q_\varepsilon - B_i$$

$$q_i = \sqrt{(W_i^2 - m_\nu^2)} \quad (i = 1,2)$$

$\eta$  can be determined from  $\lambda_i / \Lambda$  – ratio, where  $\Lambda = \frac{\ln 2}{T_{1/2}}$

# Block of tasks N1 (smallest $Q_\varepsilon$ - $B_i$ )

SHIPTRAP  
(TOF & FT)

$^{100}\text{Pd}$ - $^{100}\text{Rh}$ ,  $^{101}\text{Rh}$ - $^{101}\text{Ru}$ ,  
 $^{131}\text{Cs}$ - $^{131}\text{Xe}$ ,  $^{134}\text{Ce}$ - $^{134}\text{La}$ ,  
 $^{140}\text{Nd}$ - $^{140}\text{Pr}$ ,  $^{161}\text{Ho}$ - $^{161}\text{Dy}$ ,  
 $^{175}\text{Hf}$ - $^{175}\text{Lu}$ ,  $^{183}\text{Re}$ - $^{183}\text{W}$ ,  
 $^{194}\text{Hg}$ - $^{194}\text{Au}$

ISOLTRAP  
+JYFLTRAP

$^{77}\text{As}$ - $^{77}\text{Se}$ ,  $^{155}\text{Eu}$ - $^{155}\text{Gd}$ ,  
 $^{171}\text{Tm}$ - $^{171}\text{Yb}$ ,  $^{201}\text{Tl}$ - $^{201}\text{Hg}$ ,  
 -----  
 $^{75}\text{Se}$ - $^{75}\text{As}$ ,  $^{130}\text{Cs}$ - $^{130}\text{Ba}$ ,  
 $^{157}\text{Tb}$ - $^{157}\text{Gd}$ ,  $^{159}\text{Dy}$ - $^{159}\text{Tb}$

LEBIT

$^{44}\text{Ti}$ - $^{44}\text{Sc}$ ,  
 $^{75}\text{Se}$ - $^{75}\text{As}$

HITRAP

$^{159}\text{Dy}$ - $^{159}\text{Tb}$  and other selected pairs

Atomic physics  
calculations  
 $a_i$ ,  $B_i$ ,  $\Sigma B_i$

Gran Sasso

Levels population,  
accurate level energy

# Block of tasks N2 (neutrino mass determination)

## HITRAP

$^{163}\text{Ho}-^{163}\text{Dy}$ ,  $^{161}\text{Ho}-^{161}\text{Dy}$ ,  $^{159}\text{Dy}-^{159}\text{Tb}$



## Calorim. Lab

$\lambda_i/\lambda_j$

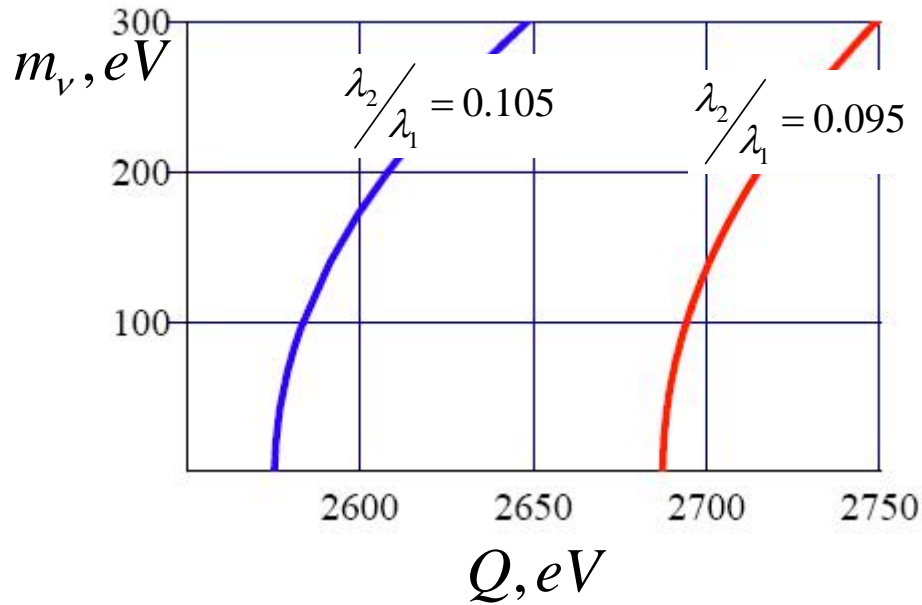
$^{163}\text{Ho}-^{163}\text{Dy}$

$\lambda_i/\sum\lambda_i$

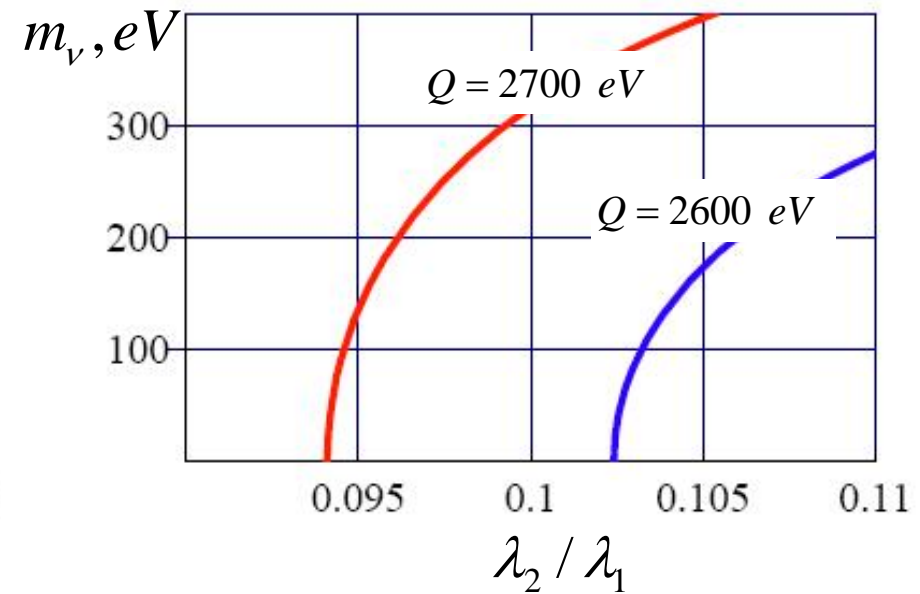
$^{161}\text{Ho}-^{161}\text{Dy}$

# Dependence of neutrino mass value on $Q_\varepsilon$ and $\lambda_{M2}/\lambda_{M1}$

Neutrino mass dependence on  $Q$ -value



Neutrino mass dependence on  $\lambda_2/\lambda_1$



# Conclusions

- masses for twenty pairs of nuclides must be measured at the conventional traps with precision better than  $10^{-8}$  ( $\sim 1$  keV),
- masses for chosen nuclides should be ultraprecisely measured at the HITRAP with precision better than  $10^{-10}$ ,
- atomic electron capture ratios should be measured as precisely as possible (e.g., for  $^{163}\text{Ho}$  it should be  $<10^{-3}$ ).

# Thanks to collaborators

## "Initiative team" in traps

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